

MATH 3A TANGENT PROBLEM AND LIMITS

I. Secant line and tangent line

What is a secant line? How do we compute its slope?

What is a tangent line? How do we compute its slope?

II. Limits

What does this expression mean?

$$\lim_{x \rightarrow a} f(x) = L$$

Finding limit numerically:

Finding limit graphically:

III. Practice

1. A ball is thrown up into the air and its height measured in feet after t seconds is given by the function $h(t) = \frac{-16}{3}t^3 + 10t$.

- Find the coordinates of the points when $t = 0$ and $t = 3$ on the graph.
- Find the slope of the secant line joining these two points.
- What quantity does the number you found in part b) represent?

2. Consider the function $f(x) = x^2 + x + 1$. Let $P = (0, 1)$ which is a point on the graph. Let $Q = (x, f(x))$ be another point on the graph.

- Find the slope of the secant line joining P and Q for the following x values.
 - $x = 0.1$
 - $x = 0.01$
 - $x = 0.001$

b) Based on your answers in part a), guess what the slope of the tangent line at P is.

c) Find the equation of the tangent line to the graph at P .

(Hint: To find equation of a line, you need the slope and a point. What is the slope of the tangent line? What is a point on the line?)

3. Below is the graph of a function $y = f(x)$.

Find the following limits (if exists) based on the graph.

- $\lim_{x \rightarrow -1} f(x) =$
- $\lim_{x \rightarrow 0} f(x) =$
- $\lim_{x \rightarrow 2} f(x) =$
- $\lim_{x \rightarrow \infty} f(x) =$