MATH 3C SOLVING FIRST-ORDER DIFFERENTIAL EQUATIONS

I. Undetermined Coefficients

When do you use undetermined coefficients?

How does it work?

Form of final solution:

How do you guess the solution?

Example. Solve the differential equation

2y' + y = t + 1

II. Integrating Factors

When do you use integrating factors?

How does it work?

Example. Solve the differential equation

$$y' + \frac{y}{t} = 4t, \ t > 0.$$

III. Practice

(Undetermined coefficients) Find the general solution to the DE

$$y' - 3y = e^{2t}$$

(Integrating factors) Find the general solution to the DE $y' + (\sin t)y = e^{\cos t}$