## Math 8: Homework 7

Read Chapter 18, Chapter 2, and Chapter 19.

**Exercises**: These will be due in two parts: Hand in Part A on Thursday, May  $26^{th}$  and Part B on Tuesday, May  $31^{st}$ .

Part A

Chapter 18: #2, #6, #8

Chapter 2: #3

**I.** Prove that the relation  $\sim$  on  $\mathbb{Z} \times (\mathbb{Z} \setminus \{0\})$  defined by  $(a, b) \sim (c, d)$  if and only if ad = bc is an equivalence relation.

**II.** Let  $a, b, c, d \in \mathbb{Q}$  be such that  $\sqrt{b}$  and  $\sqrt{d}$  are irrational. Prove that if  $a + \sqrt{b} = c + \sqrt{d}$ , then a = c and b = d. (Hint: You'll want to use Proposition 2.4(ii).)

## Part B

**Chapter 2**: #6

**Chapter 19**: #2, #4, #6