## Problem 1

Are the following statements true or false when the universe of discourse is $\mathbb{R}$ ? You must prove your answers are correct to receive credit.
(a) $\forall x \exists y\left(x^{2}=y\right)$.
(b) $\forall x \exists y\left(x=y^{2}\right)$.
(c) $\exists x \forall y(x y=0)$.
(d) $\forall x(x \neq 0 \rightarrow \exists y(x y=1))$.

## Solution

