INSTRUCTOR Paul J. Atzberger Department of Mathematics

Office Hours: TR 9:15am – 10:45am Office Hours Location: TR: 6712 South Hall;

CLASS TIMES TR 8:00am – 9:15am.

Phelps 1160

DESCRIPTION Computational approaches play an important role in many fields ranging from basic

scientific research to engineering to finance to machine learning and data science. This class will discuss both the mathematical foundations and the practical implementation of modern numerical methods. Examples also will be discussed from related applications

areas. More information can be found on the course website.

PREREQUISITES Calculus, Linear Algebra, Differential Equations, and experience programming.

TEXTBOOKS Numerical Analysis 10<sup>th</sup> Edition by R. L. Burden and J. D. Faires.

GRADING Homework 30%

Midterm 30% Final Exam / Project 40%

POLICIES Assignments will be assigned in class and posted on the course website. Prompt

submission of homeworks will be required. While no late homework will be accepted, one missed homework will be allowed without penalty. While it is permissible for you to discuss materials with classmates, the submitted homework must be your own work.

There is a policy of no video or pictures to be taken during lectures. Instead one should take notes or pay particular attention. There is also a policy of no texting, e-mailing, or social media during the class. It is hoped one is avoiding such distractions to make the most of the lectures.

EXAMS A midterm exam will be on Tuesday, May 8<sup>th</sup>.

Final exam/project.

**TOPICS** 

Initial-Value Problems for Ordinary Differential Equations

- Well-posedness of initial-value problems.
- o Euler's Method of Approximation.
- o Taylor Methods for Higher-order Approximation.
- o Runge-Kutta Methods.
- o Multistep Methods.
- o Convergence Analysis.
- o Order of Accuracy and Stability.
- o Stiff Differential Equations.

- Solving Linear Systems and Matrix Algebra
  - o Linear Algebra Review.
  - o Linear Equations.
  - o Direct Methods.
  - o Gaussian Elimination and Pivoting Strategies.
  - o Matrix Factorizations.
  - o Iterative Methods.
  - o Eigenvalues and Eigenvectors.
  - o Power Method.
  - o Approximate Solution of Linear Systems.
  - o Jacobi Iteration and Gauss-Siedel Iteration.
  - o Rates of Convergence.
  - o Conjugate Gradient Method.
  - o Preconditioners.
  - o Multigrid Methods.

## • Application Areas

- o Statistical Inference and Machine Learning.
- o Approaches in the Data Sciences.
- o Computer Graphics and Visualization.
- o Financial Modeling and Economics.
- o Simulation in Engineering and the Sciences.

WEBSITE http://atzberger.org/teaching