



# Midterm Exam Outline

Math 104C: Numerical Analysis

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## Approximation Theory

- Least Squares Approximation
  - linear least-squares
  - normal equations
  - fitting polynomials, exponentials, linearly independent functions to data
- Orthogonal Polynomials
  - normal equations
  - Gram-Schmidt orthogonalization
  - Legendre polynomials
    - recursive relations
    - approximation properties
  - Chebyshev polynomials
    - recursive relations
    - connections to trigonometric polynomials
    - approximation properties
- Power Series, Rational Function Approximation
  - Pade' approximation
  - Continued-Fraction approximation
  - Chebyshev rational approximation
  - Trigonometric Polynomials
- Fourier Transforms
  - Fourier transforms and its inverse
  - interpolation interpretation
  - Fast Fourier Transform (FFT) algorithm

## Approximating Eigenvalues

- Linear algebra
  - eigenvalues
  - similarity transforms
  - Gershgorin circle theorem
- Orthogonal matrices
  - similarity transforms
  - diagonalization
  - symmetric matrices
  - eigenvalues
- Power Method
  - finding eigenvalues and eigenvectors
  - deflation method
- Tridiagonal systems and Householder's Method
- QR Factorization, QR Algorithm
- Singular Value Decomposition (SVD)