# Francesc Castella

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## **Academic Positions**

2022-present	Associate Professor, University of California, Santa Barbara
2018 – 2022	Assistant Professor, University of California, Santa Barbara
2017 – 2019	Instructor, Princeton University
2016 – 2017	Associate Research Scholar, Princeton University
2013-2016	Hedrick Assistant Professor, University of California, Los Angeles

# Visiting Positions

Sept 2023	Professeur Invité, Université Sorbonne Paris Nord
Spring 2023	Research Member, MSRI/SLMath

# University Degrees

2013	Ph.D. in Mathematics, McGill University
	(advisor: Prof. Henri Darmon)
2009	M.Sc. in Mathematics, <b>BarcelonaTech</b>
2008	B.Sc. in Mathematics, BarcelonaTech

## **Awards and Honors**

2024 2024–2025 AMS Centennial Fellowship	
2023 CRM-ISM-AMQ Prize	
2016 Vicent Caselles Award, FBBVA-Royal Spanish Mathematical	Society
2016 Distinguished Teaching Award, UCLA	
2008 Évariste Galois Prize, Institut d'Estudis Catalans	

## **Research Grants**

2024 – 2027	PI, NSF Grant DMS-2401321
2021 – 2024	PI, NSF Grant DMS-2101458
2018 – 2021	PI, NSF Grant DMS-1801385 (DMS-1946136 after transfer to UCSB)
2016 – 2018	AMS-Simons Travel Grant

## **Publications**

25. Derived p-adic heights and the leading coefficient of the Bertolini–Darmon–Prasanna p-adic L-function.

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with C.-Y. Hsu, D. Kundu, Y.-S. Lee, and Z. Liu. Transactions of the American Mathematical Society, to appear, 35 pp.
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24. Base change and the Iwasawa Main Conjectures for GL<sub>2</sub>.

with A. Burungale and C. Skinner.

International Mathematics Research Notices IMRN, to appear, 13 pp.

23. On the Iwasawa theory of elliptic curves at Eisenstein primes.

Proceedings of ICTS workshop 'Elliptic curves and the special values of L-functions', to appear, 15 pp.

22. Nonvanishing of generalised Kato classes and Iwasawa main conjectures.

Proceedings for Massimo Bertolini's 60th birthday conference, to appear, 21 pp.

21. The diagonal cycle Euler system for  $GL_2 \times GL_2$ .

with R. Alonso and O. Rivero.

Journal de l'Institut Mathématique de Jussieu, to appear, 63 pp.

20. An anticyclotomic Euler system for adjoint modular Galois representations.

with R. Alonso and O. Rivero.

Annales de l'Institut Fourier, **75** (2025), no. 1, 291–329.

19. Perrin-Riou's main conjecture for elliptic curves at supersingular primes.

with X. Wan.

Mathematische Annalen, 389 (2024), no. 3, 2595–2636.

18. Iwasawa-Greenberg main conjecture for nonordinary modular forms and Eisenstein congruences on GU(3,1).

with Z. Liu and X. Wan.

Forum of Mathematics, Sigma, 10 (2022), e110, 90 pp.

17. On the anticyclotomic Iwasawa theory of rational elliptic curves at Eisenstein primes.

with G. Grossi, J. Lee, and C. Skinner.

Inventiones mathematicae, 227 (2022), no. 2, 517-580.

16. Class groups and local indecomposability for non-CM forms, with an appendix by H. Hida. with C. Wang-Erickson.

Journal of the European Mathematical Society JEMS, 24 (2022), no. 4, 1103-1160.

15. The Iwasawa Main Conjectures for GL<sub>2</sub> and derivatives of p-adic L-functions.

with X. Wan.

Advances in Mathematics, 400 (2022), 108266, 45 pp.

14. On the nonvanishing of generalised Kato classes for elliptic curves of rank 2.

with M.-L. Hsieh.

Forum of Mathematics, Sigma, 10 (2022), e12, 32 pp.

13.  $p^{\infty}$ -Selmer groups and rational points on CM elliptic curves.

with A. Burungale, C. Skinner, and Y. Tian.

Annales Mathématiques du Québec, Special Issue in honor of Bernadette Perrin-Riou,  $\mathbf{46}$  (2022), no. 2, 325-346.

\*Awarded the CRM-ISM-AMQ 2023 prize

12. A proof of Perrin-Riou's Heegner point main conjecture.

with A. Burungale and C.-H. Kim.

Algebra & Number Theory, 15 (2021), no. 7, 1627–1653.

11. On anticyclotomic variants of the p-adic Birch–Swinnerton-Dyer conjecture.

with A. Agboola.

Journal de Théorie des Nombres de Bordeaux, Iwasawa 2019 Special Issue, 33 (2021), no. 3.1, 629-658.

10. On the p-adic variation of Heegner points.

Journal de l'Institut Mathématique de Jussieu, 19 (2020), no. 6, 2127–2164.

9. On the p-part of the Birch-Swinnerton-Dyer formula for multiplicative primes.

Cambridge Journal of Mathematics, 6 (2018), no. 1, 1–23.

8. Heegner cycles and p-adic L-functions.

with M.-L. Hsieh.

Mathematische Annalen, 370 (2018), no. 1-2, 567-628.

7. On the exceptional specializations of big Heegner points.

Journal de l'Institut Mathématique de Jussieu, 17 (2018), no. 1, 207–240.

6. p-adic heights of Heegner points and Beilinson-Flach classes.

Journal of the London Mathematical Society, 96 (2017), no. 1, 156–180.

5. Variation of anticyclotomic Iwasawa invariants in Hida families.

with C.-H. Kim and M. Longo.

Algebra & Number Theory, 11 (2017), no. 10, 2339–2368.

4. A geometric perspective on p-adic properties of mock modular forms.

with L. Candelori.

Research in the Mathematical Sciences, 4:5 (2017), 15 pp.

3. Big Heegner points and special values of L-series.

with M. Longo.

Annales Mathématiques du Québec, Special Issue in honor of Glenn Stevens, 40 (2016), no. 2, 303–324.

2. p-adic L-functions and Euler systems: a tale in two trilogies.

with M. Bertolini, H. Darmon, S. Dasgupta, K. Prasanna, and V. Rotger.

Proceedings of the LMS Durham Symposium 2011, London Mathematical Society Lecture Note Series, 414 (2014), 52–101.

1. Heegner cycles and higher weight specializations of big Heegner points.

Mathematische Annalen, 356 (2013), no. 4, 1247-1282.

#### **Preprints**

10. An anticyclotomic Euler system of Hirzebruch–Zagier cycles I: Norm relations and p-adic interpolation.

with R. Alonso and O. Rivero.

submitted for publication, 28 pp.

- 9. A formula of Perrin-Riou and characteristic power series of signed Selmer groups. submitted for publication, 11 pp.
- 8. Exceptional zeros for Heegner points and *p*-converse to the theorem of Gross–Zagier and Kolyvagin.

submitted for publication, 12 pp.

- 7. Tamagawa number conjecture for CM modular forms and Rankin–Selberg convolutions. submitted for publication, 37 pp.
- 6. Generalized Kato classes on CM elliptic curves of rank 2.

submitted for publication, 26 pp.

5. Diagonal cycles and anticyclotomic Iwasawa theory of modular forms.

with K. T. Do.

submitted for publication, 50 pp.

4. Critical  $\Lambda$ -adic modular forms and bi-ordinary complexes.

with C. Wang-Erickson.

submitted for publication, 75 pp.

# 3. Mazur's main conjecture at Eisenstein primes.

with G. Grossi and C. Skinner. submitted for publication,  $32\,\mathrm{pp}$ .

# 2. Non-vanishing of Kolyvagin systems and Iwasawa theory.

with A. Burungale, G. Grossi, and C. Skinner. submitted for publication, 31 pp.

# 1. On the Iwasawa main conjectures for modular forms at non-ordinary primes.

with M. Çiperiani, C. Skinner, and F. Sprung. submitted for publication, 33 pp.

## **Invited Talks**

· Iwasawa 2025, Taipei	June 2025
$\cdot$ ICTS Workshop: "Automorphic Forms and the Bloch–Kato Conjecture, Bengaluru	$\mathrm{May}\ 2025$
· NCTS Number Theory Seminar, Taipei	February 2025
$\cdot$ 2025 RIMS Conference: "Automorphic forms and its arithmetic applications", Kyoto	January 2025
· UCLA, Number Theory Seminar	April 2024
$\cdot$ TSIMF Workshop: "Special values of $L\text{-functions}$ ", Sanya, China	January 2024
· Colloquium, Wayne State University	December 2023
· Number Theory Seminar, Wayne State University	December 2023
· Southern California Number Theory Day, UC Irvine	October 2023
· Université de Lille, Number Theory Seminar	September 2023
$\cdot$ Université Sorbonne Paris Nord, Number Theory Seminar (2 lectures)	September 2023
$\cdot$ Conference: "Galois Representations and Automorphic Forms", Bedlewo, Poland	August 2023
· Morningside Center of Mathematics, Beijing	June 2023
$\cdot$ MSRI/SLMath, Euler Systems Program Research Seminar	May 2023
· University of Pittsburgh, Number Theory Seminar	April 2023
$\cdot$ KIAS Instructional Workshop: "Iwasawa Theory for Automorphic Forms" (online, 3 lectures)	December 2022
· UCLA, Number Theory Seminar	November 2022
$\cdot$ The University of Texas at Austin, Number Theory Seminar	November 2022
$\cdot$ AMS Sectional Meeting, Special Session: "Iwasawa Theory", UMass Amherst	October 2022
$\cdot$ ICTS Workshop: "Elliptic Curves and Special Values of $L\text{-functions}$ " (online, 3 lectures), Bengaluru	August 2022
· Joint Columbia-CUNY-NYU Number Theory Seminar	April 2022
$\cdot$ The University of British Columbia, Iwasawa theory Virtual Seminar (online)	$March\ 2022$
· UCLA, Number Theory Seminar	January 2022
· University College Dublin, Algebra and Number Theory Seminar (online)	December 2021
$\cdot$ Conference: "L-functions and Iwasawa Theory", Roscoff, France (online)	November 2021

· Caltech, Number Theory Seminar	October 2021
· The University of British Columbia, Number Theory Seminar (online)	September 2021
· ICTS Workshop: "BSD Conjecture and Related Topics" (online, 4 lectures)	August 2021
· Mathematical Congress of the Americas (MCA) 2021, Special Session: "Galois Representations and Automorphic Forms", Buenos Aires (online)	July 2021
· 2020 CMS Summer Meeting, Special Session: "Arithmetic Geometry" (online)	June 2021
· 2020 CMS Summer Meeting, Special Session: "Algebraic Number Theory" (online)	June 2021
· LATeN, Seminario Latinoamericano de Teoría de Números (online)	April 2021
· University of Vienna, Number Theory Seminar (online)	March 2021
· Korea Institute for Advanced Study, Special Seminar (2 lectures, online)	December 2020
· University of Arizona, Number Theory Seminar (online)	October 2020
· MIT, Number Theory Seminar (online)	October 2020
$\cdot$ AMS Sectional Meeting, Special Session: "Automorphic Forms and Galois Representations", University Park (online)	October 2020
$\cdot$ 2020 CMS Summer Meeting, Special Session: "Arithmetic Geometry" (online)	June 2020
$\cdot$ 2020 CMS Summer Meeting, Special Session: "Algebraic Number Theory" (online)	June 2020
· BarcelonaTech, Number Theory Seminar (online)	May 2020
· University of Oregon, Number Theory Seminar	February 2020
· UCLA, Number Theory Seminar	February 2020
· Caltech, Number Theory Seminar	January 2020
$\cdot$ Workshop: "Congruence Ideals and $p\text{-adic }L\text{-functions}$ ", NCTS, Taipei	December 2019
· Colloquium, University of Oklahoma	November 2019
· Johns Hopkins University, Number Theory Seminar	October 2019
$\cdot$ Conference: "Recent Advances in the Arithmetic of Galois Representations", Genoa	July 2019
$\cdot$ Workshop: "Eisenstein Ideal and Iwasawa Theory", Morningside Center of Mathematics, Beijing	June 2019
$\cdot$ AMS Sectional Meeting, Special Session: "Special Values of $L\textsc{-}$ functions and Arithmetic Invariants in Families", Hartford	April 2019
$\cdot$ AMS Sectional Meeting, Special Session: "Advances in Iwasawa Theory", Honolulu	March 2019
$\cdot$ AMS Sectional Meeting, Special Session: "Algebraic Points", Honolulu	March 2019
· Québec-Vermont Number Theory Seminar, Montréal	January 2019
· Seminar, Fudan University	December 2018
· Colloquium, UC Santa Barbara	January 2018
· Colloquium, Rice University	December 2017
· Colloquium, Michigan State University	November 2017
· Colloquium, UC San Diego	November 2017
· Purdue University, Automorphic Forms Seminar	November 2017
$\cdot$ Princeton University/IAS Number Theory Seminar, Princeton	October 2017

· Conference: "Special Cycles on Shimura Varieties and Iwasawa Theory", EPFL	August 2017
· Workshop: "Euler Systems and Special Values of $L$ -functions", EPFL (3 lectures)	August 2017
· Jornadas de Teoría de Números, Lleida (plenary speaker)	June 2017
$\cdot$ Conference: "p-adic Methods for Galois Representations and Automorphic Forms", Barcelona	February 2017
· Colloquium, UC San Diego	January 2017
$\cdot$ Montréal-Toronto Workshop in Number Theory: "Mock Modular Forms and Their Relatives", Montréal	December 2016
· Columbia University, Arithmetic and Automorphic Forms Seminar	December 2016
· University of Pennsylvania, Algebra Seminar	October 2016
· BIRS Workshop: "New Directions in Iwasawa Theory", Banff	June 2016
· UCSD, Number Theory Seminar	May 2016
· Morningside Center of Mathematics, Beijing (2 lectures)	March 2016
· Colloquium, University of Arizona	January 2016
· Workshop: "Arithmetic of Euler Systems", Benasque	August 2015
· University of Chicago, Number Theory Seminar	April 2015
· Northwestern University, Number Theory Seminar	April 2015
· Workshop: " $p$ -adic Methods in the Theory of Classical Automorphic Forms", Montréal	March 2015
· Joint Mathematics Meetings, Special Session: "Selmer Groups", San Antonio	January 2015
· UC Irvine, Number Theory Seminar	October 2014
· Columbia University, Arithmetic and Automorphic Forms Seminar	September 2014
· ICM Satellite Conference: "Automorphic Forms and Arithmetic", Pohang	August 2014
$\cdot$ $p$ -adic Variation in Number Theory (Glenn Stevens' 60th), Boston University	June 2014
· Caltech, Number Theory Seminar	May 2014
· National Taiwan University (3 lectures)	February 2014
$\cdot$ IAS Program: "Special Cycles and $p\text{-adic }L\text{-functions}$ ", Hong-Kong	January 2014
· Princeton University, Number Theory Seminar	November 2013
· UCLA, Number Theory Seminar	October 2013
· Workshop: "Effective Methods for Darmon Points", Benasque	August 2013
$\cdot$ FRG/RTG mini-Conference: "p-adic Modular Forms, L-functions and Galois Representations", UCLA	May 2013
· The University of Texas at Austin, Number Theory Seminar	April 2013
· Workshop: "Iwasawa Theory and $p$ -adic Families of Automorphic Forms", Kyoto University (4 lectures)	April 2013
· 2012 CMS Winter Meeting, Special Session: "Algebraic Number Theory", Montréal	December 2012
$\cdot$ Workshop: "p-adic Langlands Program: Recent Developments and Applications", Fields Institute, Toronto	April 2012

#### Teaching Experience

#### **UCSB**

2025 Spring · Math 4A: Linear Algebra with Applications

2025 Spring · Math 220C: Modern Algebra III 2024 Fall · Math 220A: Modern Algebra I

2024 Winter • Math 225B: Topics in Number Theory: Introduction to Iwasawa Theory 2023 Fall • Math 225A: Topics in Number Theory: Elliptic Curves and Modular Forms

2023 Fall · Math 108B: Advanced Linear Algebra

2023 Winter · Math 260Q: Seminar in Mathematics: Iwasawa Theory of Elliptic Curves

2023 Winter · Math 220B: Modern Algebra II 2022 Fall · Math CS 120FN: Number Systems 2022 Winter · Math 220B: Modern Algebra II

2021 Fall · Math 4A: Linear Algebra with Applications

2021 Spring · Math 225C: Topics in Number Theory: Rational Points on Elliptic Curves 2021 Winter · Math 225B: Topics in Number Theory: Introduction to Elliptic Curves

2021 Winter  $\phantom{0}\cdot$  Math 111B: Abstract Algebra II

2020 Fall · Math 8: Transition to Higher Mathematics

2020 Spring · Math 220C: Modern Algebra III 2020 Winter · Math 220B: Modern Algebra II 2019 Fall · Math 220A: Modern Algebra I

#### Princeton

2019 Spring · MAT 419: Topics in Number Theory: Algebraic Number Theory
2018 Fall · MAT 419: Topics in Number Theory: Arithmetic of Elliptic Curves

2018 Spring · MAT 202: Linear Algebra with Applications

2017 Fall · MAT 511: Class Field Theory

2017 Spring · MAT 175: Multivariable Calculus for Economics 2016 Fall · MAT 175: Multivariable Calculus for Economics

#### **UCLA**

2016 Winter · Math 132: Complex Analysis for Applications 2015 Fall · Math 33A: Linear Algebra and Applications 2015 Fall · Math 132: Complex Analysis for Applications

2015 Spring · Math 117: Algebra for Applications

2015 Winter · Math 110A: Algebra

2015 Winter · Math 31B: Integration and Infinite Series

2014 Fall Math 207A: Topics in Number Theory: Euler Systems and BSD Conjecture

2014 Spring · Math 33A: Linear Algebra and Applications

2013 Fall · Math 115A: Linear Algebra

2013 Fall · Math 31A: Differential and Integral Calculus

#### Mentoring Experience

#### **UCSB**

2024 Spring · Pico Gilman '26. Reading course on p-adic modular forms 2024 Winter · Pico Gilman '26. Reading course on Eisenstein congruences 2023 Spring · Matthew Verheul '24. Reading course on Kato's Euler system 2023 Spring · Justin Wu '26. Reading course on p-adic Hodge theory · Sarah Mantell \*27 and Milo Moses '26. Reading course on Iwasawa theory 2022 Fall 2022-2023 · Aleix Torres \*23 (UPC-CFIS Visiting Student). Senior thesis: "Greenberg's methods on the Iwasawa theory for elliptic curves" 2021 Summer · Neel Murthy '22. Reading course on the work of Dasgupta-Kakde 2021 Spring · Neel Murthy '22. Reading course on class field theory 2021 Spring · Kyle Hansen \*24, Mychelle Parker \*24, Zach Wagner \*24, Mulun Yin \*24. Reading course on algebraic number theory 2020-2021 · Mychelle Parker \*24. Reading course on arithmetic of elliptic curves · Dylan Adams '21. Project on codimension two Iwasawa theory 2020 Summer 2020 Summer · Travis Steele '21. Project on Iwasawa theory of supersingular elliptic curves 2020 Spring · Dylan Adams '21. Reading course on homological algebra 2020 Winter · Ansuman Barbalai '21. Reading course on p-adic Hodge theory

#### Princeton

2019 Spring · Gary Hu '20. Junior paper: "Towards the 2-converse of Gross-Zagier-Kolyvagin" 2019 Spring · Casimir Kothari '20. Junior paper: "Around Goldfeld's conjecture" 2019 Spring · Dylan Galt '20. Reading course on the arithmetic of elliptic curves

2018 Summer · Gary Hu '20. Reading course on p-adic singular moduli

2018 Summer · Cooper Young '20. Reading course on p-adic singular moduli

2018 Spring · Murilo Zanarella '19. Junior paper: "Kolyvagin's conjecture for supersingular primes"

2018 Spring · Alec Leng '21. Reading course on the arithmetic of elliptic curves

2017 Summer · Ishan Levy '19. Reading course on Stark's conjectures and p-adic analogs 2017 Summer · Samuel Marks '19. Reading course on Stark's conjectures and p-adic analogs

## **UCLA**

2016 Spring · Jaehoon Lee \*19. Reading course on Euler Systems

· Van Latimer '16. Senior paper: "2-adic modular forms and Maeda's conjecture" 2015 Fall 2014 Spring · Yishu Gong '16. Junior paper: "Towards a p-adic theory of mock modular forms"

2014 Spring · Ziyi Zhuang '15. Senior paper: "p-adic properties of Taylor coefficients of modular forms"

2013 Fall · Zuhair Mullath \*17. Reading course on Algebraic Geometry

## Postdoctoral Mentees

- · Kim Tuan Do, 2025–present.
- · Raúl Alonso, 2023-present.
- · Rusiru Gambheera, 2023–present.
- · Syed Wagar Ali Shah, 2022–present.
- · Zuhair Mullath, 2021–2024.

#### PhD Students

- · Paul-Antoine Seitz, 2023-present.
- · Yi-Li Wu, 2023-present.
- · Mulun Yin, 2021–present (expected graduation: 2025).
- · Christine Alar, 2021–present (expected graduation: 2025).
- · Mychelle Parker, 2021–present (expected graduation: 2025).

## **Professional Service**

- · Organizer (with Ashay Burungale, Antonio Lei, and Christopher Skinner), BIRS Workshop: "Iwasawa Theory for GL(2) and Applications", Casa Matematica Oaxaca (August 30–September 4, 2026).
- · Organizer (with Samit Dasgupta, Eyal Goren, Adrian Iovita, Antonio Lei, Alice Pozzi, Giovanni Rosso, and Jan Vonk), Conference: "Arithmetic cycles, Modular forms, and L-functions", Centre de Recherches Mathématiques (August 18–22, 2025).
- · Co-organizer, UCSB Seminar on Geometry and Arithmetic (2019–present).
- $\cdot$  Project co-leader with Zheng Liu, APAW 2022 Collaborative Research Workshop.
- · ANID-Chile grant external reviewer.
- · ERC grant external reviewer.
- · IRC grant external reviewer.
- · NSERC grant external reviewer.
- $\cdot$  NSF panelist.
- · External reviewer for the Marie Curie COFUND project "WINNINGNormandy".
- · External reviewer for the María de Maeztu post-doctoral call.
- · Second reader for the PhD thesis of Raúl Alonso \*23 (advisor: Chris Skinner), Princeton University.
- · Second reader for the PhD thesis of Kim Tuan Do \*22 (advisor: Chris Skinner), Princeton University.
- · Chair, UCSB Algebra Hiring Committee (Fall 2024).
- · Department graduate advisor (2021–present).
- · Member, UCSB VAP Hiring Committee (Winter 2022, Winter 2023).
- · Member, UCSB Hiring Practices Committee (Winter 2021).
- · Co-organizer, Student learning seminar on Iwasawa theory for elliptic curves (Fall 2021).
- · Organizer, UCSB Mathematics Department Colloquium (Fall 2019).
- · Co-organizer, Princeton Mathematics Department Colloquium (Spring 2019).
- · Co-organizer, Princeton University/IAS Number Theory Seminar (2018–2019).
- · Projects assistant for Christopher Skinner, Arizona Winter School 2018: Iwasawa Theory.
- · Second reader for the PhD thesis of Maya Thackeray \*20 (advisor: Chris Skinner), Princeton University.
- · Second reader for the senior thesis of Murilo Zanarella '19 (advisor: Chris Skinner), Princeton University.
- · Second reader for the senior thesis of Matt Tyler '19 (advisor: Manjul Bhargava), Princeton University.
- · Reader/examiner for the senior thesis of Miranda Moore '17, Princeton University.

- $\cdot$  Co-organizer, UCLA Number Theory Seminar (2013–2016).
- $\cdot$  Organizer, UCLA Participating Number Theory Seminar (Fall 2014).

# Personal

· Birthdate: July 28, 1986

 $\cdot$  Spanish citizen and US permanent resident

Last updated: March 2025