

2 For lecture on 10/1

1. Find the domain for the following functions.

(a) $f(x, y) = \frac{\sqrt{x-2y}}{x}$.

(b) $f(x, y) = \sqrt{\frac{x-2y}{x}}$.

(c) $f(x, y) = \ln(16 - x^2 - y^2)$.

2. Find the limit of $f(x, y)$ as $(x, y) \rightarrow (0, 0)$, if it exists; or state the reason if it does not exist:

(a) $f(x, y) = \frac{x^3y - xy^3 - x}{1 - xy}$.

(b) $f(x, y) = \frac{2x^2 - y^2}{x^2 + 2y^2}$.

(c) $f(x, y) = \frac{\sin(3x^2 + y^2)}{x^2 + 2y^2}$.

(d) $f(x, y) = \frac{xy^3}{x^2 + y^6}$.

(e) * $f(x, y) = (2x^2 + y^2)e^{-\frac{1}{y^2 - 2x^2}}$.

(f) * $f(x, y) = \frac{xy}{\sqrt{x^2 + y^2}}$.

3. If $f(x, y, z) = (x - 2y, z + 3x)$ and $g(u, v) = (v, -u, \sqrt{u + v})$. Find $f \circ g$ and $g \circ f$, and state the domain for these two functions.