

Math 118: Homework 1

1. Let a and b be real numbers with $a < b$. Find the supremum and infimum of the set $S = \{x \in \mathbb{R} : (x - a)(x - b) < 0\}$.

2. Chapter 1, Exercise #5.

3. (a) For sets A and B of real numbers that are bounded above, let $a = \sup A$, $b = \sup B$ and prove that $\sup C = a + b$ where C is the set

$$C = \{x + y : x \in A, y \in B\}.$$

(b) Find sets A and B bounded above and below such that $\sup D \neq ab$ where D is the set

$$D = \{xy : x \in A, y \in B\}$$

and $a = \sup A$, $b = \sup B$.

4. (a) Chapter 1, Exercise #9.

(b) For the order defined in part (a) on the set \mathbb{C} , are the requirements (i) and/or (ii) in the definition of an ordered field true?

(c) Chapter 1, Exercise #8. This shows that no matter what order we define on the set \mathbb{C} , it will not be an ordered field.

5. Chapter 1, Exercise #6.