

# Math 118: Homework 1

**1.** Let  $a$  and  $b$  be real numbers with  $a < b$ . Find the supremum and infimum of the set  $S = \{x \in \mathbb{R} : (x - a)(x - b) < 0\}$ .

**2.** Chapter 1, Exercise #5.

**3.** (a) For sets  $A$  and  $B$  of real numbers that are bounded above, let  $a = \sup A$ ,  $b = \sup B$  and prove that  $\sup C = a + b$  where  $C$  is the set

$$C = \{x + y : x \in A, y \in B\}.$$

(b) Find sets  $A$  and  $B$  bounded above and below such that  $\sup D \neq ab$  where  $D$  is the set

$$D = \{xy : x \in A, y \in B\}$$

and  $a = \sup A$ ,  $b = \sup B$ .

**4.** (a) Chapter 1, Exercise #9.

(b) For the order defined in part (a) on the set  $\mathbb{C}$ , are the requirements (i) and/or (ii) in the definition of an ordered field true?

(c) Chapter 1, Exercise #8. This shows that no matter what order we define on the set  $\mathbb{C}$ , it will not be an ordered field.

**5.** Chapter 1, Exercise #6.