

# WORKSHEET 4

Date: 10/06/2022

Name:

## Definitions

**DEFINITION 1** (union).

**DEFINITION 2** (intersection).

**DEFINITION 3** (subset).

**DEFINITION 4** (equality of sets).

**DEFINITION 5** (Set difference).

# Practice Problems

1. Write whether each of the following statements is true or false.

(a)  $\forall p, q \in \mathbb{Q}, \exists r \in \mathbb{Q}$  such that  $p \leq r \leq q$ .

(b)  $\exists a, b \in \mathbb{R}, (a + b)^2 = a^2 + b^2$ .

(c)  $\forall m, n \in \mathbb{N}, m + n \leq m \cdot n$ .

2. Let  $A$  and  $B$  be sets. Prove that  $A \cup B = B$  if and only if  $A \subseteq B$ .

- (a) Write down the givens/assumptions in this statement. Its a biconditional statement so you should do these steps twice.
- (b) What is the goal? Write down what you want to prove.
- (c) Prove the statement above.

3. Let  $A = \{ (\frac{1}{9})^n \mid n \in \mathbb{N} \}$ , and let  $B = \{ (\frac{1}{3})^n \mid n \in \mathbb{N} \}$

(a) Prove that  $A \subseteq B$ .

(b) Is  $A$  also a proper subset of  $B$ ? if so, why?