

WORKSHEET [π]

Date: 06/23/2022

Name:

PROOFS AND COUNTER-EXAMPLES

As the title suggests, we will go over proofs and counter-examples of statements in section today. I found a web-page which goes over basic proof techniques. I suggest you click the following link and explore the page. I would love to go over this in section, but unfortunately we don't have enough time. [Click me please.](#)



PERFECT PROOF PRACTICE

Break into groups and construct a proof for the following questions. Your group will volunteer one represented, Squid Game style, to attempt a proof on the chalkboard.

1. If $C \subseteq A$, $D \subseteq B$, and A and B are disjoint, then C and D are disjoint.

[Recall: two sets are disjoint if their intersection is empty i.e. $A \cap B = \emptyset$]

2. If $A \cup B \subseteq C \cup D$, $A \cap B = \emptyset$, and $C \subseteq A$, then $B \subseteq D$.

3. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be a function. We say that f is *bounded*, if

(B) there is $M > 0$ such that $|f(x)| \leq M$ for all $x \in \mathbb{R}$

- (a) Write down the negation of the statement (B) as a complete sentence.

- (b) Give an example of a bounded function.

(c) Show that your example in (b) is bounded.

(d) Give an example of a function that is not bounded.

(e) Show that your example in (d) is not bounded.

4.

THEOREM 1. *e is irrational.*