

Homework 3: Nontransitive Dice

1 New Problems

1. Using the list of cyclotomic polynomials in the notes, can you classify all of the pairs of nonstandard k -dice that have the same sum probability as a pair of standard k -dice? Assume that we're working with typical physical dice here, so that our values of k are limited to the platonic solids (with 4,6,8,12, or 20 sides.)
2. What about triples of k -dice? I.e. are there triples of nonstandard k -dice with the same sum probability as a triple of standard k -dice?
3. What if we relax our condition to simply looking for a collection of two dice (not necessarily with the same number of sides) that has the same sum probability as a pair of k -dice? I.e. are there ways of combining a nonstandard octahedral die and a nonstandard tetrahedral die to get the same sum probability as a pair of cubical dice?
4. Consider the above problem again, except look for triples instead of pairs.